

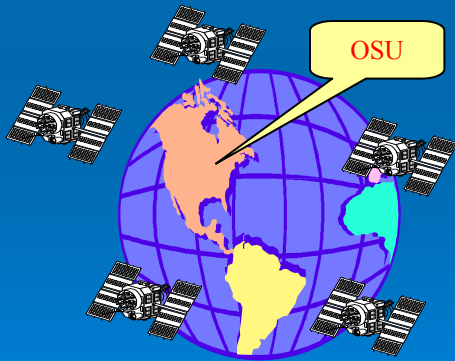
Towards Real-time Geometric Orbit Determination of Low Earth Orbiters

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Outline

- Precise Kinematic Orbit Determination (P-KOD) with triple differences
- Performance analysis: CHAMP
- Data screening (CS detection)
- Orbit smoothing
- Achievable accuracy
- Summary

Kinematic POD

■ Advantages

- No force model error affects the solution
- Fast (potential for near real-time)
- Quality solution for good PDOP

■ Disadvantages

- No dynamics to compensate for weak geometry
- No solution or weak solution for weak geometry
- Requires correct coordinates for a starting epoch (forward solution only)

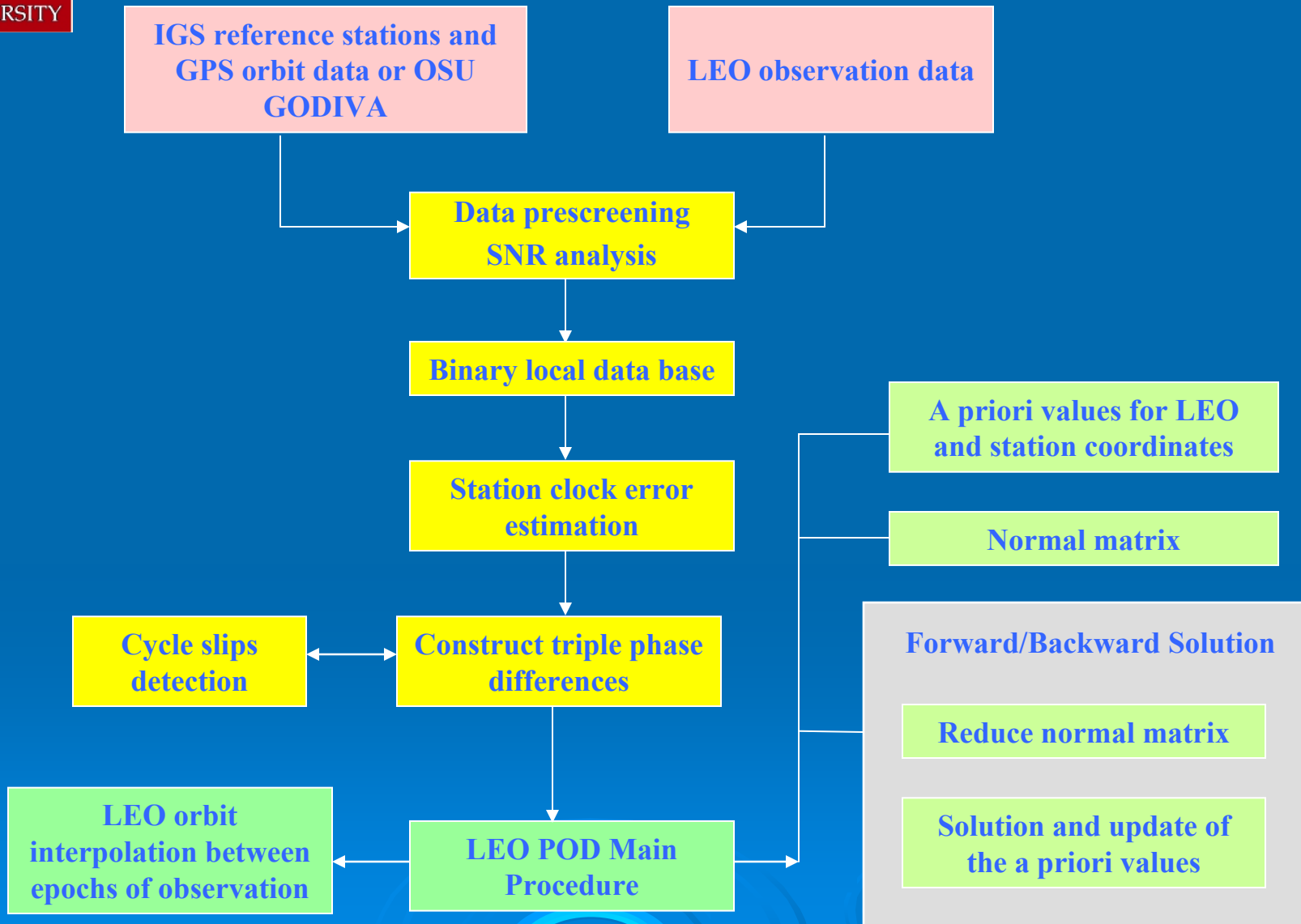
Triple Difference POD

- Primary advantage: fast, no ambiguity fixing
- Disadvantage: epoch-to-epoch correlation (non-diagonal variance-covariance matrix)
 - Cholesky decomposition and decorrelation scheme
- Requires good approximated orbit to detect CS (large residuals)
- Equivalent to double difference with float ambiguities

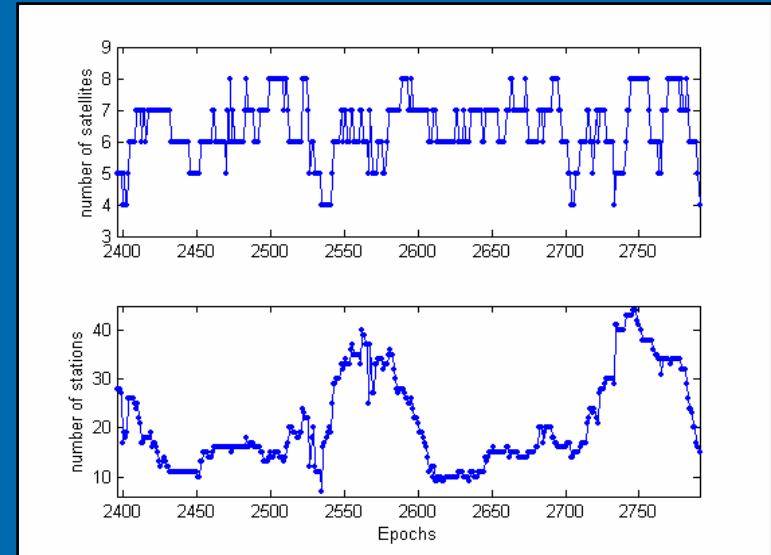
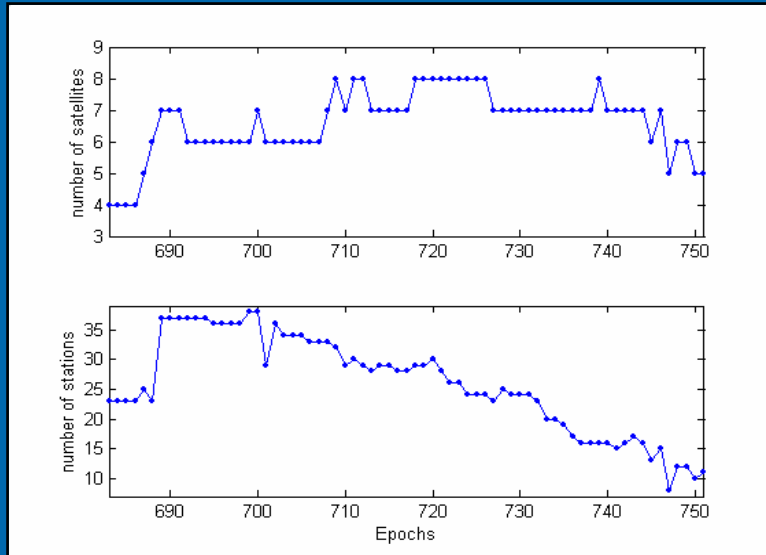
P-KOD Data Processing: CHAMP

- 24 hour data sets processed
 - 65 IGS tracking stations
 - 30-s data sampling rate
 - Elevation cut off angle 0° (CHAMP) and 10° (stations)
- CS detection based on initial SNR prescreening, and triple difference residual analysis
- Normal matrix is accumulated until a singularity point is reached (too few observations or bad geometry)
- Initial epoch released (forward/backward filter)

P-KODE Processing Flowchart



Examples of Weak Geometry



Epochs	RMS _x [m]	RMS _y [m]	RMS _z [m]	RMS _{3D} [m]	No. of Iterations
0683:0751 (068)	0.111	0.075	0.266	0.298	13
2396:2791 (395)	0.265	0.179	0.351	0.475	2

Statistics of Singularities

No.	Duration	# of epochs
1	0253 ~ 0255	3
2	0678 ~ 0682	5
3	0752 ~ 0753	2
4	1080 ~ 1080	1
5	1314 ~ 1314	1
6	1392 ~ 1392	1
7	1904 ~ 1904	1
8	2394 ~ 2395	2
9	2792 ~ 2792	1
SUM		17

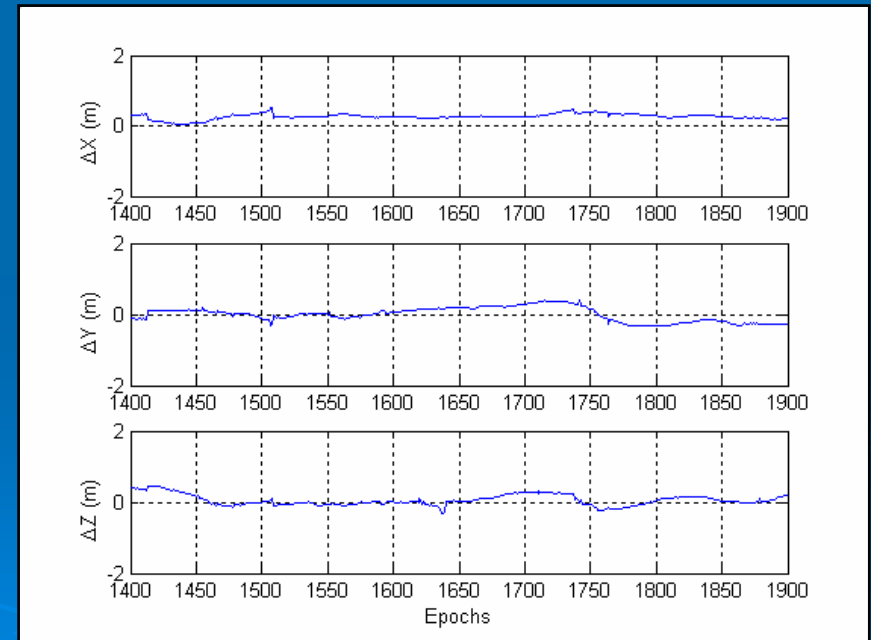
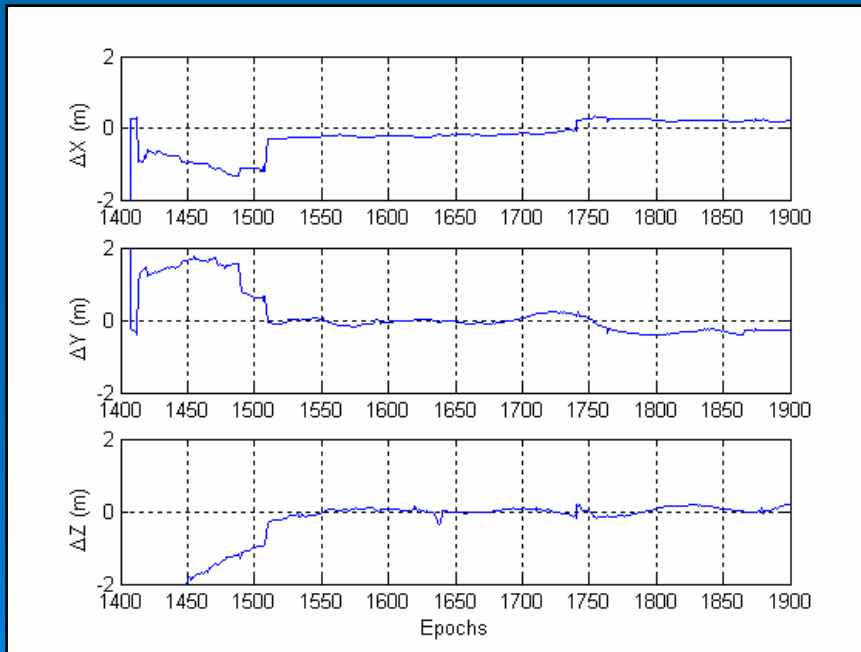
Example Results : June 15, 2001

Forward filter solution

$RMS_x = 0.513 \text{ m}$
 $RMS_y = 0.865 \text{ m}$
 $RMS_z = 1.059 \text{ m}$
 $RMS_{3D} = 1.460 \text{ m}$

Backward filter solution

$RMS_x = 0.079 \text{ m}$
 $RMS_y = 0.202 \text{ m}$
 $RMS_z = 0.155 \text{ m}$
 $RMS_{3D} = 0.266 \text{ m}$



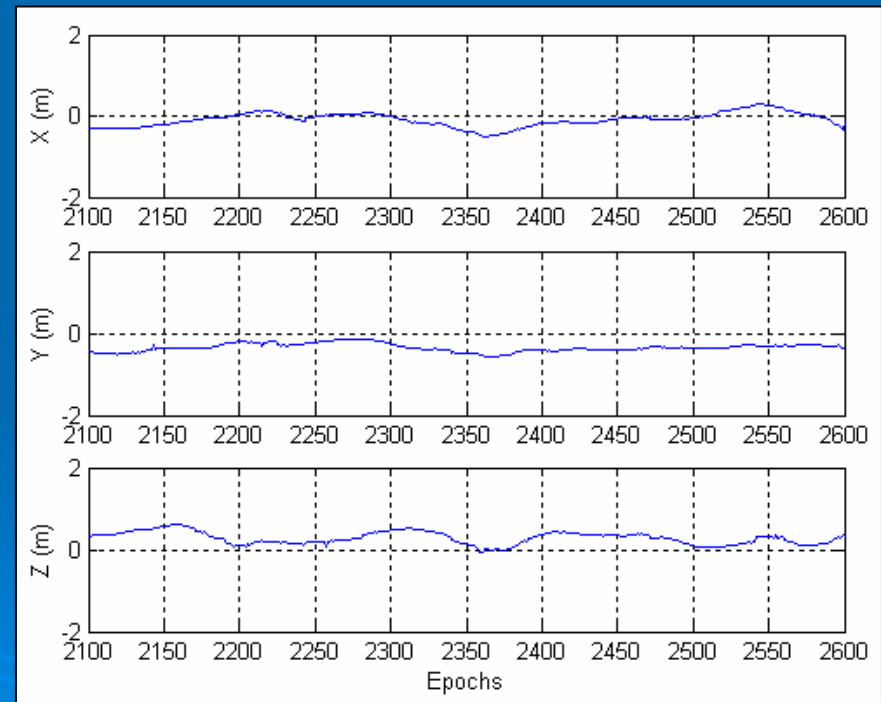
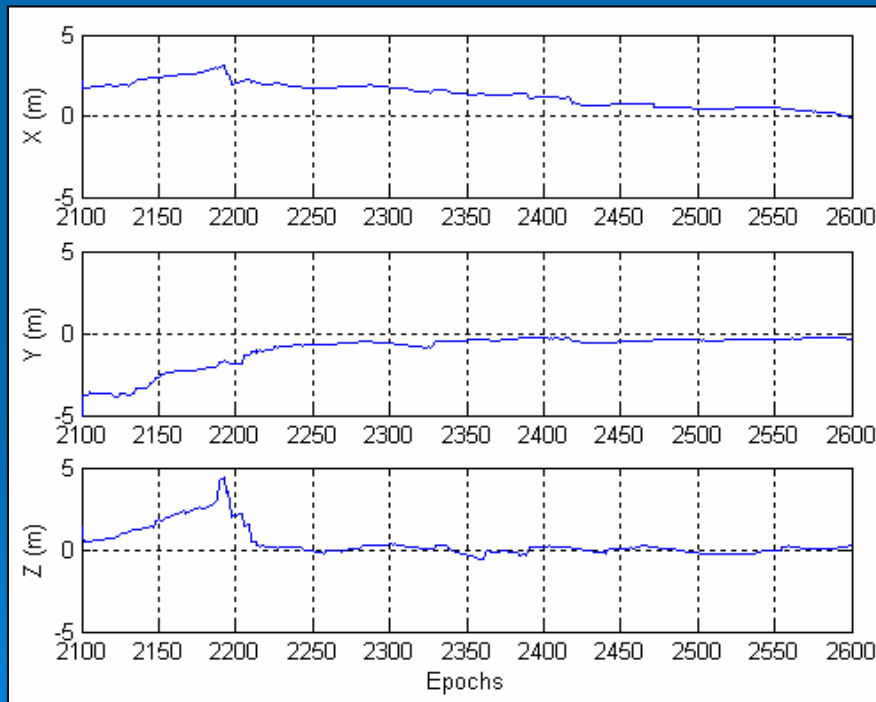
Example Results: October 3, 2001

Forward filter solution

$RMS_x = 0.745 \text{ m}$
 $RMS_y = 1.029 \text{ m}$
 $RMS_z = 0.866 \text{ m}$
 $RMS_{3D} = 1.537 \text{ m}$

Backward filter solution

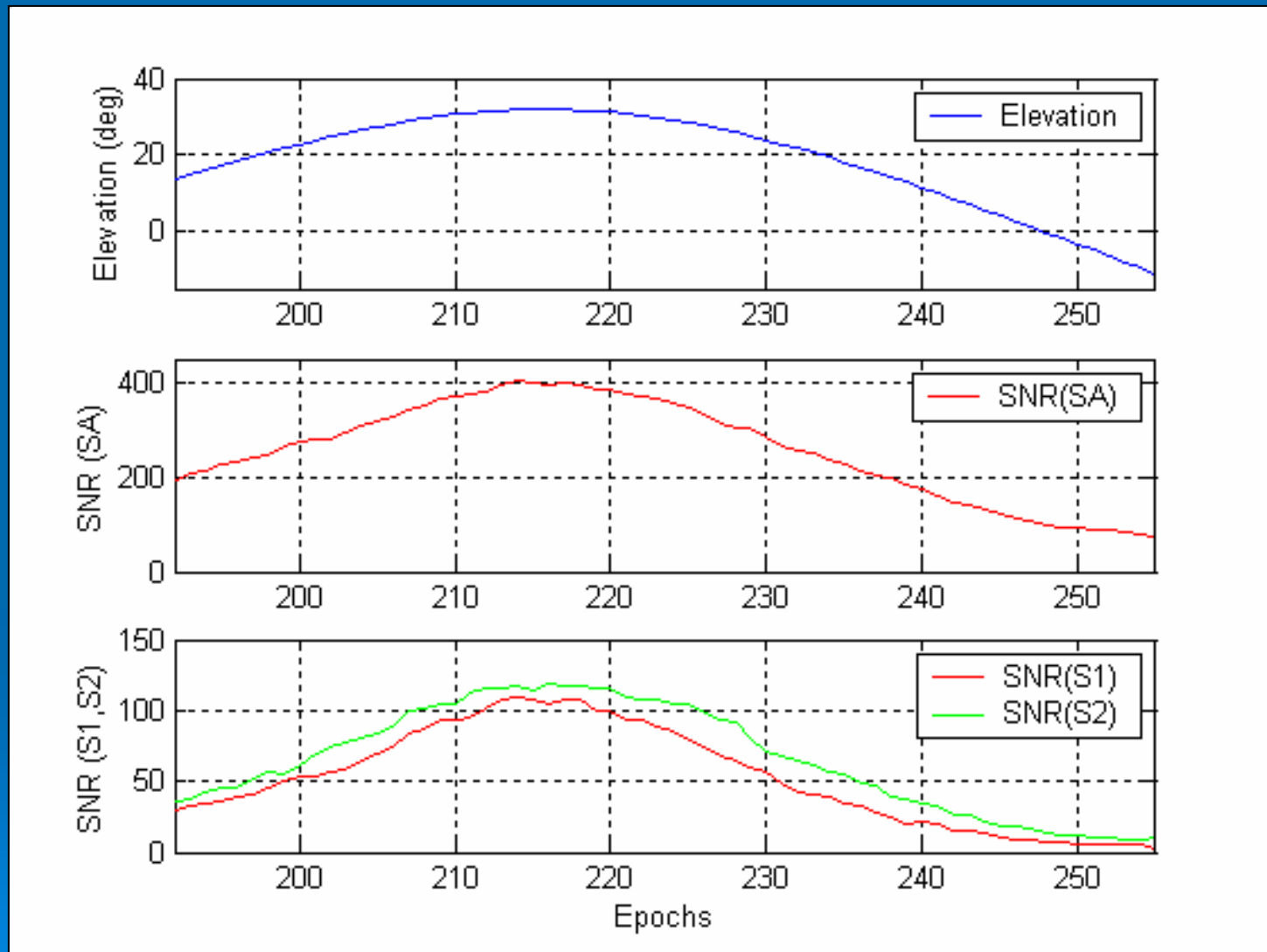
$RMS_x = 0.173 \text{ m}$
 $RMS_y = 0.098 \text{ m}$
 $RMS_z = 0.154 \text{ m}$
 $RMS_{3D} = 0.252 \text{ m}$



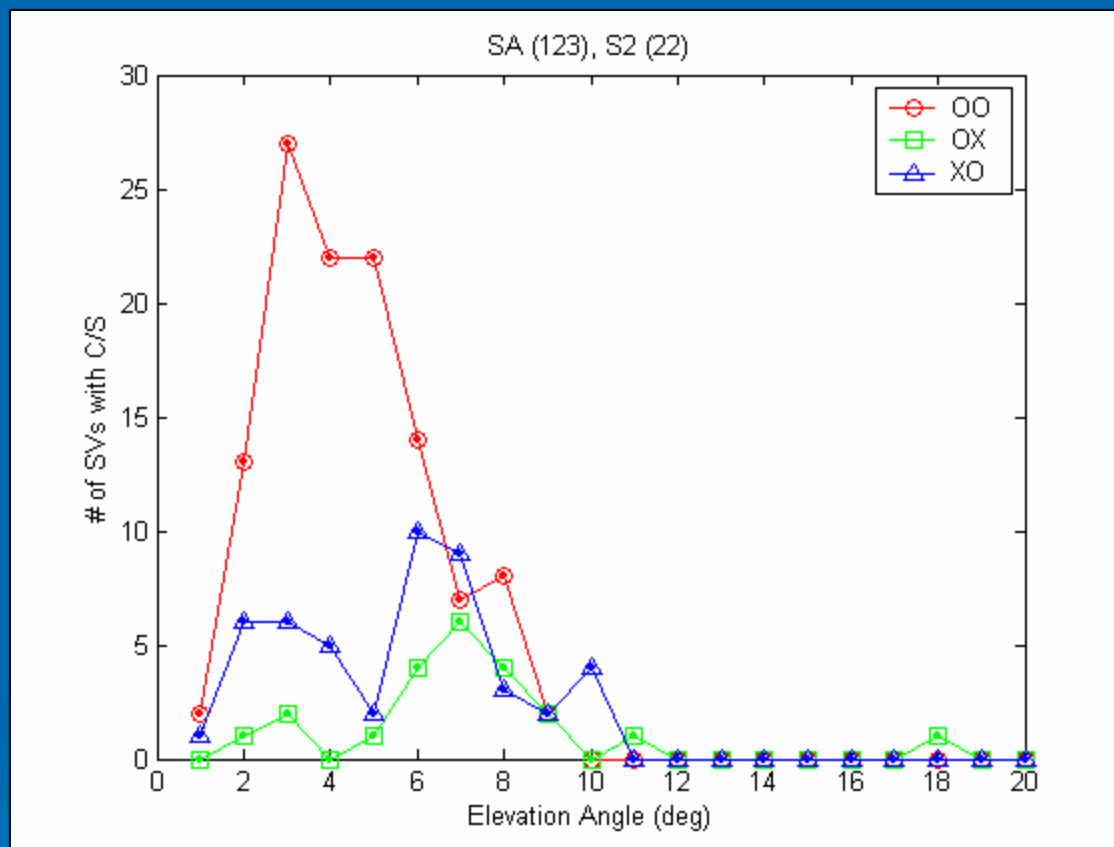
SNR for CS Detection

- CS caused by low SNR due to bad ionospheric conditions, multipath, high receiver dynamics or low elevation angle
- Raw signal strength
- 3 types of SNR
 - S1, S2 : L1, L2 phase observations
 - SA : SNR for C/A channel (CHAMP ext.)
- Related to the elevation angle

SNR vs. Elevation



Cycle Slip Detection Using SNR: CHAMP



- **OO – C/S detected by both methods (TD residual and SNR)**
- **OX – C/S indicated by TD residual only**
- **XO – C/S indicated by SNR only**

Cycle Slip Detection Using SNR: CHAMP

SA	S2	# of C/S	# of matched C/S
120	22	1708 (5.0%)	1336 (80.6%)
121	22	1817 (5.3%)	1354 (81.7%)
122	22	1910 (5.7%)	1372 (82.8%)
123	22	1938 (5.6%)	1395 (84.2%)
124	22	1984 (5.8%)	1415 (85.4%)
125	22	2099 (6.1%)	1417 (85.5%)

- **Number of C/S in TD residuals: 1657**
- **Total number of TD: 34374**
- **500 epochs tested, all PRNs included**

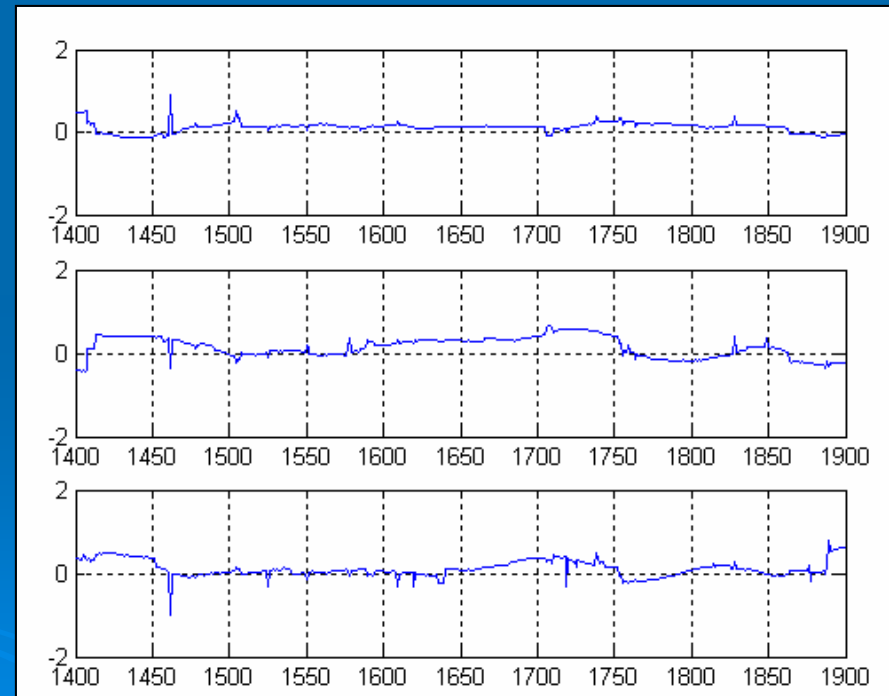
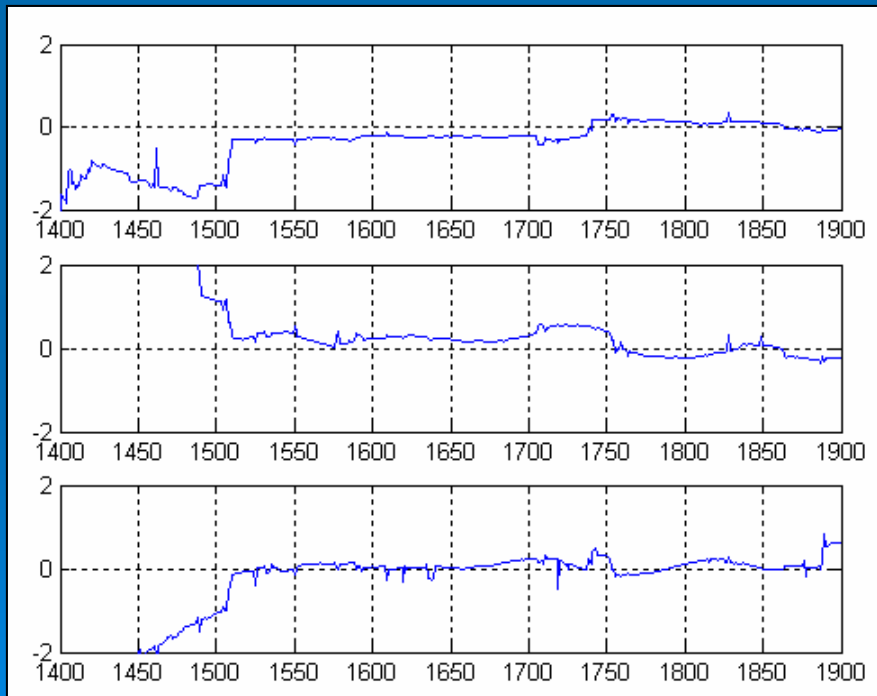
Corresponding Orbit Solution: initial approximation good to ~ 5 m

Forward filter solution

$RMS_x = 0.538$ m
 $RMS_y = 1.014$ m
 $RMS_z = 1.223$ m
 $RMS_{3D} = 1.677$ m

Backward filter solution

$RMS_x = 0.120$ m
 $RMS_y = 0.245$ m
 $RMS_z = 0.193$ m
 $RMS_{3D} = 0.334$ m



Orbit Smoothing

- Guerra and Tapia (1974)
 - built-in FORTRAN function
 - works for the data with less than 25% error
- Moving averaging window
 - average of 20 data points
- Polynomial Fitting
 - 9th order

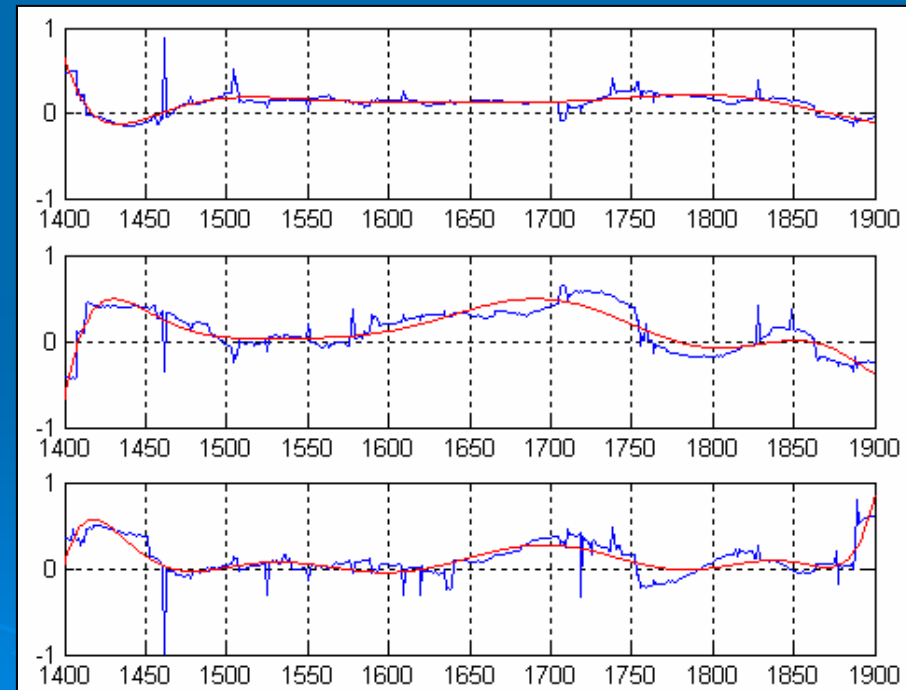
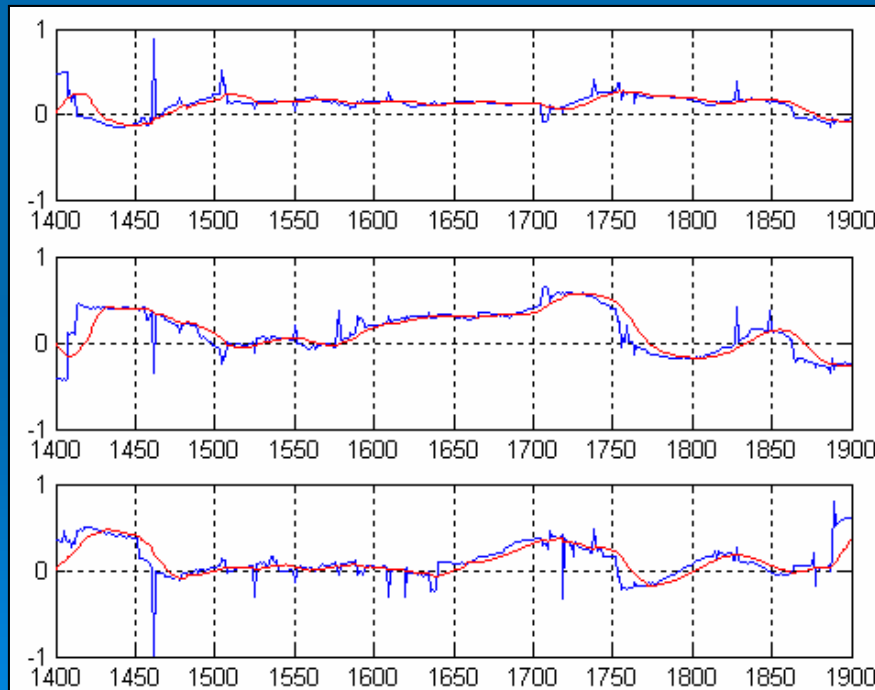
Orbit Smoothing

Direct Form II Transposed

$RMS_x = 0.092 \text{ m}$
 $RMS_y = 0.220 \text{ m}$
 $RMS_z = 0.154 \text{ m}$
 $RMS_{3D} = 0.283 \text{ m}$

Polynomial fitting (n=9)

$RMS_x = 0.099 \text{ m}$
 $RMS_y = 0.213 \text{ m}$
 $RMS_z = 0.154 \text{ m}$
 $RMS_{3D} = 0.280 \text{ m}$



Summary

- Kinematic triple difference POD works well for good geometry
- Short processing time (less than 2 h, forward and backward, on 1.8 GHz Pentium processor)
- Problems with weak geometry
- CS cleaning is not easy (high dynamics, LEO in the middle of the ionospheric layer)
 - SNR plus orbit smoothing give promising results
 - More work needs to be done on SNR threshold selection
- Gaps in the solution – reduced dynamics needed for orbit continuity and balance between geometry and force model